

©Martin Osborne and Ariel Rubinstein. These **lecture notes** are distributed for the exclusive use of students in Tel Aviv University, 2005. They are basically inserts from our book *A Course of Game Theory*, MIT Press 1994 combined with some additional comments.

---

## **Problem set for Lecture G-10: Repeated Games**

**Readings: Osborne and Rubinstein Ch 11**

---

**Exercise 1:** Consider the game form in figure 216.1 in the book.

Find the behavioral strategy of player 1 that is equivalent to his mixed strategy in which she plays  $(B, r)$  with probability 0.4,  $(B, l)$  with probability 0.1 and  $(A, l)$  with probability 0.5.

**Exercise 2:** Consider the zero sum game with imperfect recall in Figure 217.1. Show that player 1's best behavioral strategy assures his payoff of 1 with probability  $1/4$ , while there is a mixed strategy that assure him the payoff 1 with probability 1.

**Exercise 3:** Let  $\Gamma_2$  be an extensive game with imperfect information in which there are no chance moves, and assume that the game  $\Gamma_1$  differs from  $\Gamma_2$  only in that one of the information sets of player 1 in  $\Gamma_2$  is split into two information sets in  $\Gamma_1$ . Show that all Nash equilibrium in pure strategies in  $\Gamma_2$  correspond to Nash equilibria of  $\Gamma_1$ . Show that the requirement that there be no chance moves is essential for the result.

**Exercise 4:** Formulate the following parlor game as an extensive game with imperfect information. First player 1 receives a card that is either  $H$  or  $L$  with equal probabilities. Player 2 does not see the card. Player 1 may announce that his card is  $L$ , in which case he must pay \$1 to player 2, or may claim that his card is  $H$ , in which case player 2 may choose to concede or to insist on seeing player 1's card. If player 2 concedes then he must pay \$1 to player 1. If player 2 insists on seeing player 1's card then player 1 must pay him \$4 if his card is  $L$  and player 2 must pay player 1 \$4 if his card is  $H$ .

**Exercise 5:** Consider an absent-minded driver who, in order to get home, has to take the highway and get off at the second exit. Turning at the first exit leads into a bad neighborhood (payoff 0). Turning at the second exit yields the highest reward

(payoff 4). If he continues beyond the second exit, he will have to go a very long way before he can turn back home (payoff 1). The driver is absent-minded and is aware of this fact. When reaching an intersection, his senses do not tell him whether he is at the first or the second intersection; that is, he cannot remember how many intersections he has passed.

Formulate the situation as a one player game.

Show that the best behavioral strategy is better than the best mixed strategy.

Show that the best behavioral strategy is not time consistent.